

MATHEMATICS AND STATISTICS (MST)

MST 605. Applied Multivariable Mathematics. (3 h)

Introduction to several topics in applied mathematics including complex numbers, probability, matrix algebra, multivariable calculus, and ordinary differential equations. May not be used toward any graduate degree offered by the department.

MST 606. Advanced Mathematics for the Physical Sciences. (3 h)

Advanced topics in linear algebra, special functions, integral transforms, and partial differential equations. May not be used toward any graduate degree offered by the department. P-MTH 605.

MST 611. Introductory Real Analysis I. (3 h)

Limits and continuity in metric spaces, sequences and series, differentiation and Riemann-Stieltjes integration, uniform convergence, power series and Fourier series, differentiation of vector functions, implicit and inverse function theorems.

MST 612. Introductory Real Analysis II. (3 h)

Limits and continuity in metric spaces, sequences and series, differentiation and Riemann-Stieltjes integration, uniform convergence, power series and Fourier series, differentiation of vector functions, implicit and inverse function theorems.

MST 617. Complex Analysis I. (3 h)

Analytic functions Cauchy's theorem and its consequences, power series, and residue calculus.

MST 622. Modern Algebra II. (3 h)

A continuation of modern abstract algebra through the study of additional properties of groups, rings, and fields.

MST 624. Linear Algebra II. (3 h)

A thorough treatment of vector spaces and linear transformations over an arbitrary field, canonical forms. inner product spaces, and linear groups.

MST 626. Numerical Linear Algebra. (3 h)

An introduction to numerical methods for solving matrix and related problems in science and engineering using a high-level matrix-oriented language such as MATLAB. Topics include systems of linear equations, least squares methods, and eigenvalue computations. Special emphasis is given to applications.

MST 631. Geometry. (3 h)

An introduction to axiomatic geometry including a comparison of Euclidean and non-Euclidean geometries.

MST 634. Differential Geometry. (3 h)

Introduction to the theory of curves and surfaces in two and three dimensional space including such topics as curvature, geodesics, and minimal surfaces.

MST 645. Elementary Number Theory. (3 h)

Course topics include properties of integers, congruences, and prime numbers, with additional topics chosen from arithmetic functions, primitive roots, quadratic residues, Pythagorean triples, and sum of squares.

MST 646. Modern Number Theory. (3 h)

Course topics include a selection of number-theory topics of recent interest. Some examples include elliptic curves, partitions, modular forms, the Riemann zeta function, and algebraic number theory.

MST 647. Graph Theory. (3 h)

Paths, circuits, trees, planar graphs, spanning trees, graph coloring, perfect graphs, Ramsey theory, directed graphs, enumeration of graphs and graph theoretic algorithms.

MST 648. Combinatorial Analysis I. (3 h)

Enumeration techniques, generating functions, recurrence formulas, the principle of inclusion and exclusion, Polya theory, graph theory, combinatorial algorithms, partially ordered sets, designs, Ramsey theory, symmetric functions, and Schur functions.

MST 649. Combinatorial Analysis II. (3 h)

Enumeration techniques, generating functions, recurrence formulas, the principle of inclusion and exclusion, Polya theory, graph theory, combinatorial algorithms, partially ordered sets, designs, Ramsey theory, symmetric functions, and Schur functions.

MST 651. Introduction to Mathematical Modeling. (3 h)

Introduction to the mathematical modeling, analysis and simulation of continuous processes using MATLAB, Mathematica or Maple. Topics include dimensional analysis, stability analysis, bifurcation theory, one-dimensional flows, phase plane analysis, index theory, limit cycles, chaotic dynamics, hyperbolic conservation laws and traveling waves.

MST 652. Partial Differential Equations. (3 h)

Detailed study of partial differential equations, including the heat, wave, and Laplace equations, using methods such as separation of variables, characteristics, Green's functions, and the maximum principle.

MST 654. Discrete Dynamical System. (3 h)

Introduction to the theory of discrete dynamical systems as applied to disciplines such as biology and economics. Includes methods for finding explicit solutions, equilibrium and stability analysis, phase plane analysis, analysis of Markov chains and bifurcation theory.

MST 655. Introduction to Numerical Methods. (3 h)

An introduction to numerical computations on modern computer architectures; floating point arithmetic and round-off error including programming in a scientific/engineering language such as MATLAB, Cor Fortran. Topics include algorithms and computer techniques for the solution of problems such as roots of functions, approximations, integration, systems of linear equations and least squares methods. Also listed as CSC 655.

MST 657. Probability. (3 h)

Distributions of discrete and continuous random variables, sampling distributions. Covers much of the material on the syllabus for the first actuarial exam. This course is cross-listed as STA 610.

MST 658. Mathematical Statistics. (3 h)

This course will cover derivation of point estimators, hypothesis testing, and confidence intervals using both maximum likelihood and Bayesian approaches. P - MST 657 or POI.

MST 681. Individual Study. (1, 2 h)

A course of independent study directed by a faculty adviser. By prearrangement. May be repeated for credit.

MST 682. Reading in Statistics. (1-3 h)

Reading in statistical topics to provide a foundational basis for more advanced study in a particular area. May not be used to satisfy any requirement in the MA degree with thesis. No more than three hours may be applied to the requirements for the MA degree without thesis. May be repeated for credit for a total of 3 hours.

MST 683. Advanced Topics in Mathematics. (1-3 h)

Topics in mathematics that are not considered in regular courses. Content varies.

MST 711. Real Analysis. (3 h)

Measure and integration theory, elementary functional analysis, selected advanced topics in analysis.

MST 712. Real Analysis. (3 h)

Measure and integration theory, elementary functional analysis, selected advanced topics in analysis.

MST 715. Seminar in Analysis. (1 h)**MST 716. Seminar in Analysis. (1 h)****MST 717. Optimization in Banach Spaces. (3 h)**

Banach and Hilbert spaces, best approximations, linear operators and adjoints, Frechet derivatives and nonlinear optimization, fixed points and iterative methods,. Applications to control theory, mathematical programming, and numerical analysis.

MST 718. Topics in Analysis. (3 h)

Selected topics from functional analysis or analytic function theory.

MST 721. Abstract Algebra. (3 h)

Groups, rings, fields, extensions, Euclidean domains, polynomials, vector spaces, Galois theory.

MST 722. Abstract Algebra. (3 h)

Groups, rings, fields, extensions, Euclidean domains, polynomials, vector spaces, Galois theory.

MST 723. Seminar on Theory of Matrices. (1 h)**MST 724. Seminar on Theory of Matrices. (1 h)****MST 725. Seminar in Algebra. (1 h)****MST 726. Seminar in Algebra. (1 h)****MST 728. Topics in Algrbra. (3 h)**

Topics vary and may include algebraic coding theory, algebraic number theory, matrix theory, representation theory, non-commutative ring theory.

MST 731. Topology. (3 h)

Point-set topology including topological spaces, continuity, connectedness, compactness, and metric spaces. Additional topics in topology may include classification of surface, algebraic topology, and knot theory.

MST 732. Topics in Topology and Geometry. (3 h)

Topics vary and may include knot theory, algebraic topology, differential topology, manifolds, and Riemannian geometry. May be repeated for credit. P - 731 or POI.

MST 735. Seminar on Topology. (1 h)**MST 736. Seminar on Topology. (1 h)****MST 737. Seminar in Geometry. (1 h)****MST 738. Seminar on Geometry. (1 h)****MST 744. Topics in Number Theory. (3 h)**

Topics vary and are chosen from the areas of analytic, algebraic, and elementary number theory. Topics may include Farey fractions, the theory of partitions, Waring's problem, prime number theorem, and Dirichlet's problem.

MST 745. Seminar on Number Theory. (1 h)**MST 746. Seminar on Number Theory. (1 h)****MST 747. Topics in Discrete Mathematics. (3 h)**

Topics vary and may include enumerative combinatorics, graph theory, algebraic combinatorics, combinatorial optimization, coding theory, experimental designs, Ramsey theory, Polya theory, representational theory, set theory and mathematical logic.

MST 748. Seminar on Combinatorial Analysis. (1 h)**MST 749. Sem on Combinatorial Analysis. (1 h)****MST 750. Dynamical Systems. (3 h)**

Introduction to modern theory of dynamical systems. Linear and nonlinear autonomous differential equations, invariant sets, closed orbits, Poincare maps, structural stability, center manifolds, normal forms, local bifurcations of equilibria, linear and non-linear maps, hyperbolic sets, attractors, symbolic representation, fractal dimensions. P - MST 611.

MST 752. Topics in Applied Mathematics. (3 h)

Topics vary and may include computational methods in differential equations, optimization methods, approximation techniques, eigenvalue problems. May be repeated for credit.

MST 753. Nonlinear Optimization. (3 h)

The problem of finding global minimums of functions is addressed in the context of problems in which many local minima exist. Numerical techniques are emphasized, including gradient descent and quasi-Newton methods. Current literature is examined and a comparison made of various techniques for both unconstrained and constrained optimization problems. Credit no allowed for both MST 753 and CSC 753. P - MST 655 or CSC 655.

MST 754. Numerical Methods for Partial Differential Equations. (3 h)

Numerical techniques for solving partial differential equations (including elliptic, parabolic, and hyperbolic) are studied along with applications to science and engineering. Theoretical foundations are described and emphasis is placed on algorithm design and implementation using either C, FORTRAN, or MATLAB. Credit not allowed for both MST 754 and CSC 754. P-MST 655 or CSC 655.

MST 757. Stochastic Processes and Applications. (3 h)

This course includes the axiomatic foundations of probability theory and an introduction to stochastic processes. Applications may include Markov chains, Markov Chain Monte Carlo with Metropolis-Hastings, Gibb sampling, Brownian motion, and related topics, with an emphasis on modern developments. This course is cross-listed as STA 710. P-MST 657 or STA 610 and MST 611 or POI.

MST 791. Thesis Research I. (1-9 h)

May be repeated for credit. Satisfactory/Unsatisfactory.

MST 792. Thesis Research II. (1-9 h)

May be repeated for credit. Satisfactory/Unsatisfactory.